

الكهربائية والمغناطيسية

التاريخ ٧ / ١١ / ٢٠١٩

الموضوع :

١- المتجهات Vectors

٢- الكهرباء الساكنة Electrostatic

٣- قانون كولوم Coulumb's law

٤- المجال الكهربائي Electric field

٥- الفيض الكهربائي، وقانون جاوس electric flux

٦- الجهد الكهربائي electric Potential ~~بالدقة~~

٧- المكثفات Capacitors

٨- التيار والمقاومة Current Resistance

٩- دوائر التيار المستمر Direct current

١٠- المغناطيسية

الكميات

متجهة

Vector

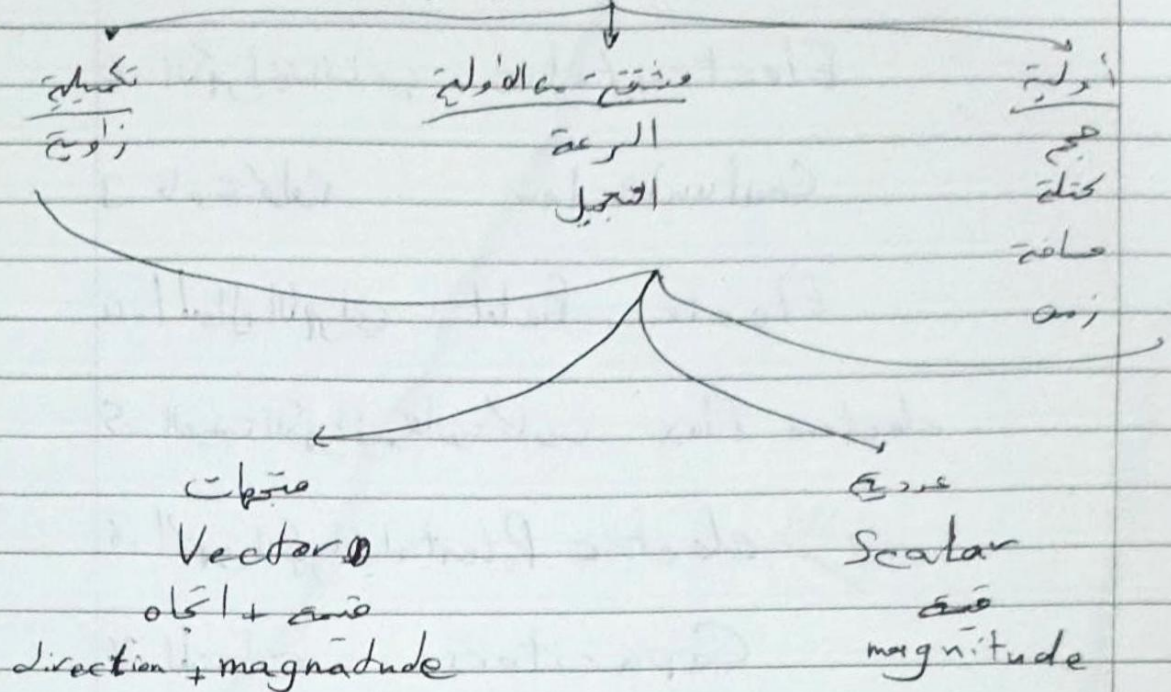
(قيمة واتجاه)

عددية

Scalar

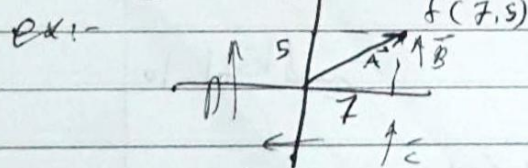
(قيمة)

الكميات الفيزيائية



Rectangular Coord.

الدعامات الكارتيزية

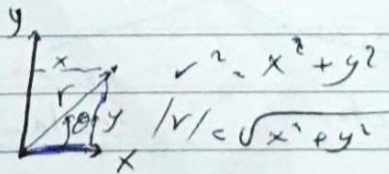


x, y

x, y, z

Polar Coord.

(2) الدعامات القطبية



$$\begin{cases} x = r \cos \theta \\ y = r \sin \theta \end{cases}$$

$$\begin{cases} \sin \theta = \frac{y}{r} \\ \cos \theta = \frac{x}{r} \end{cases} \Rightarrow \tan \theta = \frac{y}{x}$$

Example: If the vector coordinate of a vector are $(x, y) = (-3.5, -2.5)$

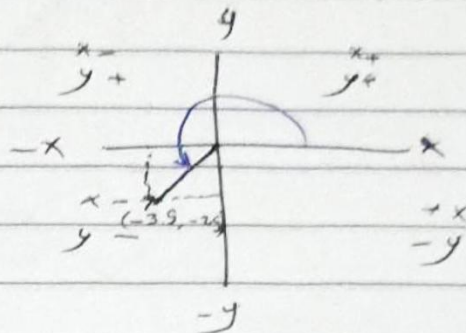
Find his polar coordinate

r, θ

$$r = \sqrt{x^2 + y^2}$$

$$= \sqrt{(-3.5)^2 + (-2.5)^2}$$

$$= 4.3 \text{ m}$$



$$\tan \theta = \frac{y}{x} = \frac{-2.5}{-3.5} = 0.714$$

$$\theta = \tan^{-1}(0.714) = 216^\circ$$

Ex: Find the Value of the vector (r) and it's direction (θ) if $x = 3 \text{ m}$ and $y = 4 \text{ m}$

$$r = \sqrt{x^2 + y^2} = \sqrt{9 + 16} = \sqrt{25}$$

$$= \boxed{5 \text{ m}}$$

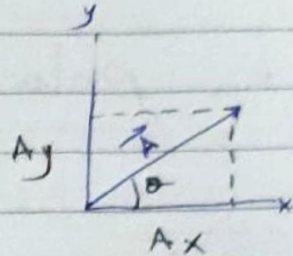
$$\tan \theta = \frac{y}{x} = \frac{4}{3} = 1.33$$

$$\tan^{-1} 1.33 = \boxed{53.13^\circ}$$

$$\frac{3}{4} = \frac{3}{4} = 53$$

Vector $\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$

$\hat{i}$ (x direction) $\hat{j}$ (y direction) $\hat{k}$ (z direction)
 1 unit $\hat{i}$ $\hat{j}$ $\hat{k}$



$$A_x = A \cos \theta$$

$$A_y = A \sin \theta$$

$$A = \sqrt{A_x^2 + A_y^2}, \theta = \tan^{-1} \frac{A_y}{A_x}$$

Vector Unit:-

وحدة المتجه

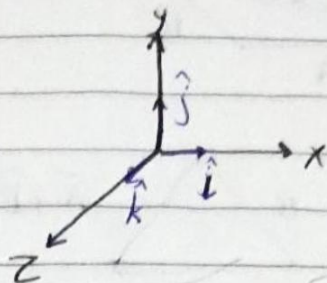
هو مقدار متجه المثلث واحد، وله يتغير مع أي مركبة متجه

لكن يُبدل كل اتجاهها ويستخدم لكتابة متجهات

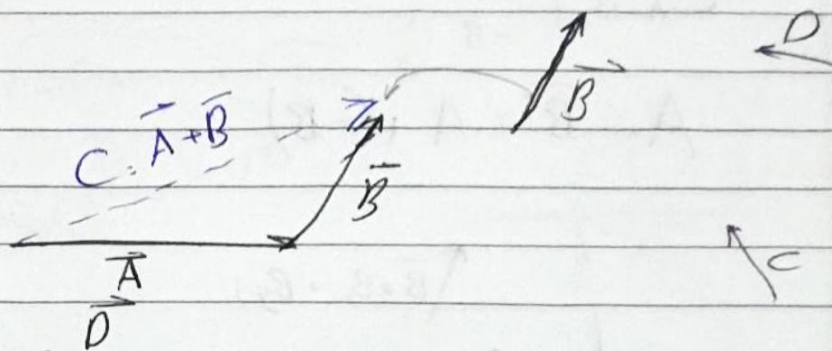
Vector Unit:- is a vector whose absolute value is one that doesn't change the amount of any component of the vector but indicates the direction and is used to write

The equation of vectors as follows

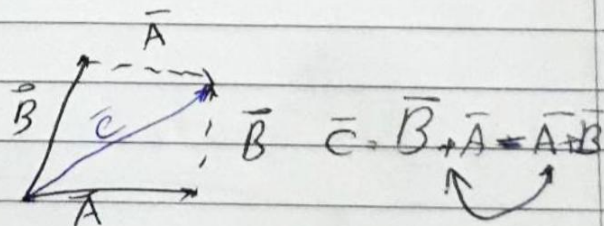
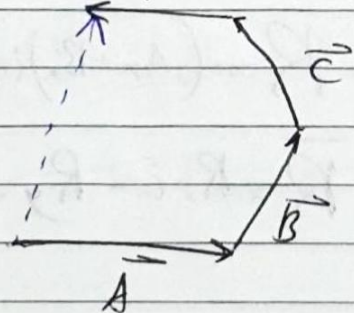
$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$



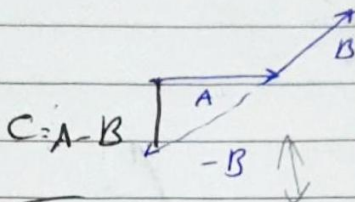
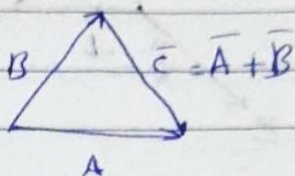
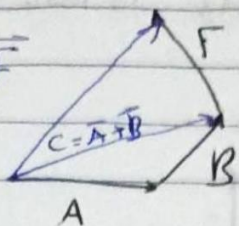
Vectors Algebra



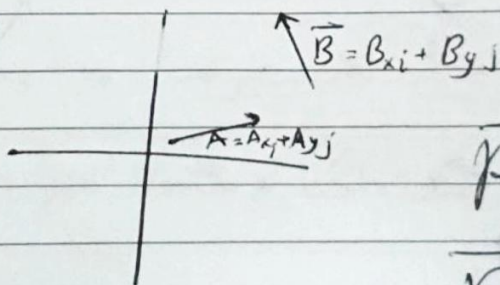
$$\vec{F} = \vec{A} + \vec{B} + \vec{C} + \vec{D}$$



$$\vec{D} = (\vec{A} + \vec{B}) + \vec{F}$$



$$\vec{A} - \vec{B} = \vec{A} + (-\vec{B})$$



$$\vec{R} = (A_x + B_x)\vec{i} + (A_y + B_y)\vec{j}$$

$$\vec{R} = R_x \vec{i} + R_y \vec{j}$$

ex: find the sum of 2 vectors

$$\vec{A} = 3\vec{i} + 4\vec{j}$$

$$\vec{B} = 2\vec{i} - 5\vec{j}$$

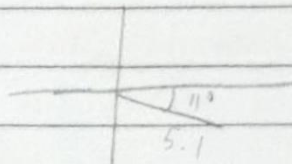
$$\vec{R} = (A_x + B_x) + (A_y + B_y)$$

$$= (3+2)\vec{i} + (4-5)\vec{j}$$

$$\vec{R} = 5\vec{i} - \vec{j}$$

$$|\vec{R}| = \sqrt{25+1} = \sqrt{26}$$

$$\theta = \tan^{-1} \frac{R_y}{R_x} = -11^\circ$$



Ex

what is the force of repulsion

between two protons in the nucleus of

Fe atom.

if the distance between the protons
is 1.5×10^{-15} m?

Find the sum of the Vector

$$\vec{A} = 2i + 2j$$

$$\vec{B} = 2i - 4j$$

$$\vec{R} = 4i - 2j$$

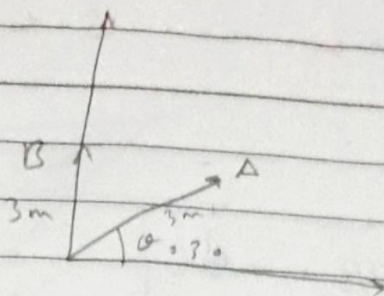
$$|\vec{R}| = \sqrt{16 + 4} = \sqrt{20}$$

$$\theta = \tan^{-1} \frac{y}{x} = \frac{-2}{4} = \frac{-1}{2} = -26.56$$

2

$$A_x = A \cos \theta$$

$$= 3(0.966) = 2.5 \text{ m}$$



$$A_y = A \sin \theta = 3\left(\frac{1}{2}\right) = \frac{3}{2} = 1.5 \text{ m}$$

$$\vec{A} = 2.5 \hat{i} + 1.5 \hat{j}$$

$$\vec{B} = 0 \hat{i} + 3 \hat{j}$$

$$\vec{R} = 2.5 \hat{i} + 4.5 \hat{j}$$

$$|\vec{R}| = \sqrt{6.25 + 20.25} = \sqrt{26.5} = 5.14 \text{ m}$$

Ex $\bar{A} = 3i - 2j$

$\bar{B} = -6 - 4j$

Find:

a) $\bar{A} + \bar{B} = \boxed{2i - 6j}$

b) $\bar{A} - \bar{B} = \boxed{4i + 2j}$

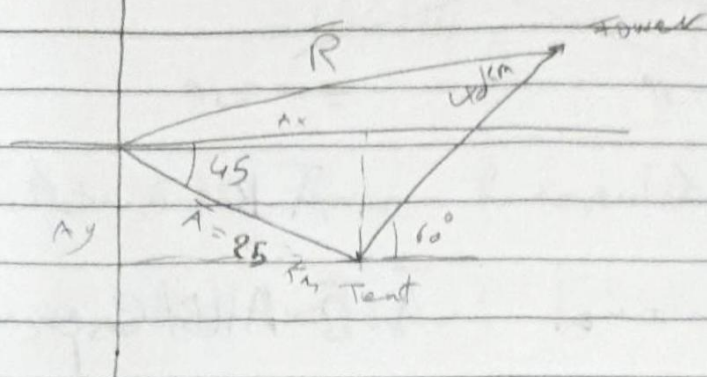
c) $|\bar{A} + \bar{B}| = \sqrt{4 + 36} = \sqrt{40} \approx 6.32$

d) $|\bar{A} - \bar{B}| = \sqrt{16 + 4} = \sqrt{20} \approx 4.47$

e) the direction of $\bar{A} + \bar{B}$ and $|\bar{A} - \bar{B}|$

$\bar{A} + \bar{B} \Rightarrow \tan^{-1} \frac{y}{x} = \frac{-6}{2} = -3 \Rightarrow \tan^{-1}(-3) = \boxed{-71.56^\circ}$

$|\bar{A} - \bar{B}| \Rightarrow \tan^{-1} \frac{y}{x} = \frac{2}{4} = \frac{1}{2} \Rightarrow \tan^{-1}(\frac{1}{2}) = \boxed{26.56^\circ}$



$$A_x = A \cos \theta = 25 \cos 315 = 17.67$$

$$A_y = A \sin \theta = 25 \sin 315 = -17.67$$

$$B_x = B \cos \theta = 40 \cos 60 = 20$$

$$B_y = B \sin \theta = 40 \sin 60 = 34.64$$

$$\therefore \vec{A} = 17.67\mathbf{i} - 17.67\mathbf{j}$$

$$\vec{B} = 20 + 34.64\mathbf{j}$$

$$\therefore \vec{R} = 37.67\mathbf{i} + 16.97\mathbf{j}$$

$$|\vec{R}| = \sqrt{x^2 + y^2} = \sqrt{1419 + 282.1} = \boxed{41.24 \text{ m}}$$

$$\tan \theta = \frac{16.97}{37.67} = \boxed{24.25^\circ}$$

Product of Vectors

جزء اتجاهي

جزء عددي

$$\vec{A} \times \vec{B} \Rightarrow \text{كيفية الاتجاهي}$$

$$\vec{A} \cdot \vec{B} \Rightarrow \text{كيفية العددية}$$

$$\vec{A} \cdot \vec{B} = A||B||\cos\theta$$

$$+ve \Leftarrow 0 < \theta < 90$$

$$-ve \Leftarrow 90 < \theta < 180$$

$$\text{Zero} \Leftarrow 90^\circ$$

$$\vec{A} = A_x \hat{i} + A_y \hat{j} + A_z \hat{k}$$

$$\vec{B} = B_x \hat{i} + B_y \hat{j} + B_z \hat{k}$$

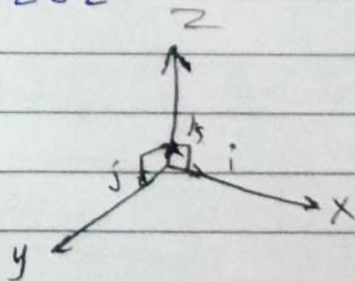
$$\vec{A} \cdot \vec{B} = (A_x \hat{i} + A_y \hat{j} + A_z \hat{k}) (B_x \hat{i} + B_y \hat{j} + B_z \hat{k})$$

$$= A_x B_x + A_y B_y + A_z B_z$$

$$\hat{i} \cdot \hat{i} = 1$$

$$\hat{j} \cdot \hat{j} = 1$$

$$\hat{k} \cdot \hat{k} = 1$$



$$\cos 90^\circ = 0$$

$$\theta = 90$$

$$\hat{i} \cdot \hat{j} = 0$$

$$\hat{j} \cdot \hat{k} = 0$$

$$\hat{k} \cdot \hat{i} = 0$$

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التابع

: Equival

$$\cos \theta = \frac{A \cdot B}{|A| |B|}$$

$$A_x B_x + A_y B_y + A_z B_z$$

$$|A| |B|$$